- 1. A stone is thrown straight up from the top of a building with initial velocity 40 ft/sec and hits the ground 4 seconds later. The height of the building in feet is:
 - a. 88 b. 96 c. 112 d. 128 e. 144
- 2. If a car accelerates from 0 to 60 mph in 10 seconds, what distance does it travel in those 10 seconds? (assume the acceleration is constant and note that 60 mph = 88 ft/sec)
 - a. 40 ft b. 44 ft c. 88 ft d. 400 ft e. 440 ft
- 3. If the velocity of a car traveling in a straight line at time t is v(t), then the difference in its odometer readings between times t = a and t = b is:

a.
$$\int_{a}^{b} |v(t)| dt$$
 b. $\int_{a}^{b} v(t) dt$

- c. the net displacement of the car's position from t=a to t=b.
- d. the change in the car's position from t=a to t=b.
- e. none of these.

4. If an object is moving up and down along the y-axis with velocity v(t) and s'(t) = v(t), then it is false that $\int_{a}^{a} v(t)dt$ gives:

- a. s(b) s(a)
- b. the net distance traveled by the object between t=a and t=b.
- c. the total change in s(t) between t=a and t=b.
- d. The shift in the object's position from t=a and t=b.
- e. The total distance covered by the object from t=a and t=b.
- 5. The function f(x) which satisfies the equations f(x)f'(x) = x and f(0) = 1 is:
 - a. $f(x) = \sqrt{x^2 + 1}$ b. $f(x) = \sqrt{1 x^2}$ c. f(x) = x
 - d. $f(x) = e^x$ e. None of these
- 6. The curve that passes through the point (1,1) and whose slope at any point (x,y) is equal to $\frac{3y}{x}$ has the equation:

a.
$$3x-2=y$$
 b. $y^3 = x$ c. $y = |x^3|$ d. $3y^2 = x^2 + 2$ e. $3y^2 - 2x = 1$

7. If
$$\frac{dy}{dx} = \frac{y}{2\sqrt{x}}$$
 and y = 1, when x = 4, then:
a. $y^2 = 4\sqrt{x} - 7$ b. $\ln y = 4\sqrt{x} - 8$ c. $\ln y = \sqrt{x-2}$ d. $y = e^{\sqrt{x}}$ e. $y = e^{\sqrt{x}-2}$

8. If
$$\frac{dy}{dx} = e^y$$
 and $y = 0$ when $x = 1$, then

a.
$$y = \ln|x|$$
 b. $y = \ln|2-x|$ c. $e^{-y} = 2-x$ d. $y = -\ln|x|$ e. $e^{-y} = x-2$

9. If $\frac{dy}{dx} = \frac{x}{\sqrt{9+x^2}}$ and y = 5 when x = 4, then:

a.
$$y = \sqrt{9 + x^2} - 5$$
 b. $y = \sqrt{9 + x^2}$ c. $y = 2\sqrt{9 + x^2} - 5$

d.
$$y = \frac{\sqrt{9 + x^2 + 5}}{2}$$
 e. None of these

- 10. If a substance decomposes at a rate proportional to the amount of the substance present, and if the amount decreases from 40 gm to 10 gm in 2 hours, then the constant of proportionality is:
 - a. $-\ln 2$ b. $-\frac{1}{2}$ c. $-\frac{1}{4}$ d. $\ln \frac{1}{4}$ e. $\ln \frac{1}{8}$
- 11. A cup of coffee at temperature 180°F is placed on a table in a room at 68°F. The differential equation for its temperature at time t is $\frac{dy}{dx} = -0.11(y 68)$; y(0) = 180. After 10 minutes, the temperature

(in °F) of the coffee is:

- a. 96 b. 100 c. 105 d. 110 e. 115
- 12. Approximately how long does it take the temperature of the coffee in question 11 to drop to 75°F?
 - a. 10 min b. 15 min c. 18 min d. 20 min e. 25 min
- 13. According to Newton's law of cooling, the temperature of an object decreases at a rate proportional to the difference between its temperature and that of the surrounding air. Suppose a corpse at temperature 32° C arrives at a mortuary where the temperature is kept at 10° C. Then the differential equation satisfied by the temperature T of the corpse *t* hours later is:

0.050

a.
$$\frac{dT}{dt} = -k(T-10)$$

b. $\frac{dT}{dt} = k(T-32)$
c. $\frac{dT}{dt} = 32e^{-kt}$
d. $\frac{dT}{dt} = -kT(T-10)$
e. $\frac{dT}{dt} = kT(T-32)$

14. If the corpse in Question 13 cools to 27°C in 1 hour, then its temperature is given by the equation:

a.
$$T = 22e^{0.205t}$$

b. $T = 10e^{1.163t}$
c. $T = 10 + 22e^{-0.258t}$
d. $T = 32e^{-0.169t}$
e. $T = 32 - 10e^{-0.093t}$

15. The population of a city increases continuously at a rate proportional, at any time, to the population at that time. The population doubles in 50 years. After 75 years, the ratio of the population P to the initial population P_0 is:

a.
$$\frac{9}{4}$$
 b. $\frac{5}{2}$ c. $\frac{4}{1}$ d. $\frac{2\sqrt{2}}{1}$ e. None of these